

Symmetry of Molecules and Group Theory (Hagiwara)

Problem Set #4(For Chapter 5&6) 2019/11/27

1. Prove that the direct product of any two 2 x 2 matrices has a trace equal to the product of the traces of the 2 x 2 matrices.
2. In determining vibrational selection rules we shall need to determine whether integrals of the type:

$$\int \psi_v^0 f \psi_v^1 d\tau$$

are nonzero, where the function f is $x, y, z, x^2, y^2, z^2, xy, yz, zx$, or any combinations or sets thereof. Also, ψ_v^0 is totally symmetric and ψ_v^1 may belong to any irreducible representation. Identify the irreducible representations to which may belong in order to give nonzero integrals for molecules of symmetry C_{4v} and D_{3d} .

3. Work out the molecular orbitals of bifluoride anion (HF_2^- , $D_{\infty h}$) following the procedure below.
 - (1) Taking account a linear arrangements of the three atomic orbitals, $s_{\text{H}}, p_{\text{F1}}, p_{\text{F2}}$, obtain the representations of them.
 - (2) Construct the secular determinant for the LCAO's.
 - (3) Show that the energy level of bonding and antibonding orbital based on LCAO's is expressed by $[(\alpha s_{\text{H}} + \alpha p) \pm \{(\alpha s_{\text{H}} - \alpha p)^2 + 4\beta^2\}^{1/2}] / 2$, where αs_{H} and αp are Coulomb integrals of s orbital of hydrogen atom and p_z orbitals of fluorine atoms and β is a resonance integral for s_{H} and p_z orbitals.
 - (4) Draw the molecular orbital energy diagram and show the electron configuration.